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# Vibrational Energy Relaxation and Dissociation in N<sub>2</sub>

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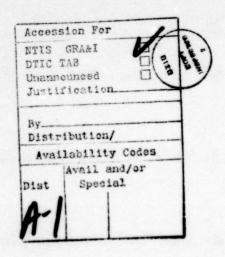
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## VIBRATIONAL ENERGY RELAXATION AND DISSOCIATION IN N2

## 1. INTRODUCTION

In a nitrogen plasma ( $N_2$ ) a fair portion of the electron energy is stored in the vibrational mode of the molecules. This energy storage occurs as a result of the electron impact excitations of the various vibrational levels of the molecule, i.e. e-V transitions, as well as by the collisions between the molecules themselves. These collisions result in the energy exchange between the vibrational and translational modes of the molecules, i.e. V-T transitions. The vibrational energy distribution, however, is also affected by the vibrational energy exchange between the molecules through the V-V transitions.

The vibrational energy in a nitrogen plasma has two interesting channels through which the energy is expended, albiet at different time scales. These channels are: the dissociation of the molecule through the vibrational ladder and the other is the vibrational relaxation to the gas kinetic mode. Nitrogen plasmas can be generated by various means, such as microwave and electric discharges, shock waves and by intense electron beams. However, several intrinsic questions arise in such plasmas, namely, what is the vibrational distribution or the vibrational temperature? How rapidly a distribution is established? What are the roles of various processes in the establishment of a vibrational temperature? What is the rate of the molecular dissociation via the vibrational ladder? How does this rate compare with the direct plasma electron dissociation of the molecule?

Vibrational relaxation studies are numerous  $^{1-3}$  with the main interest foccused on the effects of the V-T and V-V transitions on the relaxation times in different gases and gaseous mixtures. The effects of the V-V transitions on the molecular dissociation has also been considered  $^3$ , and a study  $^4$  of the relaxation and dissociation in  $^4$ 2 with the combined effects of e-V, V-T and V-Manuscript approved March 20, 1984.

V processes has been performed. No detailed studies for such relaxations has been made in  $N_2$  and air, however, some results for air have been reported<sup>5</sup>.

In this paper we present a detailed study of the relaxation and dissociation of  $N_2$  and attempt to answer the various questions raised earlier. We do this by solving a master equation described in Section II where e-V, V-T and V-V transitions are considered with different electron and gas temperatures. The appropriate rate coefficients, for the processes included in the master equation, are discussed in Section III, and the results of the calculations are presented in Section IV.

## 2. BASIC EQUATIONS

We consider the nitrogen molecule as a harmonic oscillator with a vibrational energy spacing  $^6$  of  $\sim 0.30$  eV and solve for the time development of 32 vibrational levels where the last level gives the density of the dissociated molecules. The processes that control the time histories of the vibrational levels are:

(a) The excitation and de-excitation of the vibrational level by electron impact, i.e.

$$e + N_2(v) + N_2(w) + e$$
 (1)

Here,  $N_2(v)$  indicates the population density of level v.

(b) The excitation and de-excitation of the vibrational level by collisions with molecules resulting in the vibrational-translation energy exchange, i.e. V-T transitions.

$$N_2(v) + M + N_2(v + 1) + M$$
 (2)

Where M is the total density of the molecules.

(c) The vibrational-vibrational transitions, i.e.

$$N_2(v) + N_2(w) + N_2(v+1) + N_2(w-1)$$
 (3)

Where only a single vibrational quantum is exchanged.

The master equation which governs the population density of each vibrational level, except for level 32, is

$$\frac{dN_{2}(v)}{dt} = \sum_{w=1}^{\Sigma} N_{v+1} N_{w-1} P_{v+1,v}^{w-1,w} - \sum_{w=1}^{\Sigma} N_{v} N_{w} P_{v,v+1}^{w,w-1}$$

$$- \sum_{w=0}^{\Sigma} N_{v} N_{w} P_{v,v-1}^{w,w+1} + \sum_{w=0}^{\Sigma} N_{v-1} N_{w+1} P_{v-1,v}^{w+1,w}$$

$$+ \sum_{w=0}^{\Sigma} N_{v} N_{w} N_{wv} - \sum_{w=0}^{\infty} N_{v} N_{w} N_{v} Y_{vw}$$

$$- \sum_{v=0}^{\infty} N_{v} M_{v} R_{v,v+1} + \sum_{w=0}^{\infty} N_{w} M_{v} S_{w,w-1}$$
(4)

Here  $P_{v+1,v}^{w-1,w}$  indicates the rate coefficient for the vibrational-vibrational energy exchange, i.e, the V-V transitions. Under this process a molecule at the (v+1) level loses one vibrational quantum and descends to level v while the molecule at the (w-1) vibrational level gains the vibrational quantum and

ascends to level w. The electron impact excitation resulting in the molecular transition from level w to v is indicated by  $X_{wv}$ . The corresponding deexcitation rate is given by  $Y_{vw}$ . On the other hand, the rate coefficient for the vibrational translational-collisions, i.e. V-T transitions, resulting in a vibrational excitation is represented by  $R_{v,v+1}$  and the corresponding reverse process is indicated by  $S_{w,w-1}$ .

The equation that describes the population density of level 32 is similar to Eq. 4 with the condition that the inverse processes which depopulate level 32 are not allowed.

## 3. RATE COEFFICIENTS

The electron impact rate coefficient for the vibrational excitation is obtained from the measured cross sections  $^{7,8}$ . These cross sections for transitions from v=o to v=8 have been averaged  $^{9}$  with the electron velocity over a Maxwellian electron velocity distribution and the rate coefficients are shown in Fig. 1.

For electron impact excitations to levels above v=8 we utilize the following often used  $^4$  relation,

$$X_{\mathbf{v}, \mathbf{v} + \Delta \mathbf{v}} = X_{\mathbf{0}, \Delta \mathbf{v}} \tag{5}$$

The electron impact de-excitation rate coefficient,  $Y_{V,W}$  is obtained from the corresponding excitation rate by the principle of the detailed balance, i.e.,

$$Y_{v,w} = X_{w,v} \text{ Exp [- 0.3 (v-w)/T}_{e}]$$
 (6)

where  $T_{\rm e}$  is the electron temperature in eV.

The vibrational-translational rate coefficients  $S_{w,w-1}$  is obtained from the de-excitation rate of v=1 state,  $S_{10}$ , and the harmonic oscillator relation i.e.

$$S_{v+\Delta v,v} = (v+\Delta v) S_{10}$$
 (7)

where(10)

$$S_{10} = 8.5 \times 10^{-7} \text{ Exp } \left(-\frac{12.4}{(T_q)^{1/3}}\right)$$
 (8)

Here  $T_g$  is the gas temperature in units of eV. It should be noted that relation (8) is valid for the temperature range of  $T_g$ =0.086 eV to 0.43 eV On the other hand, for V-T excitations, one has

$$R_{v,v+\Delta v} = (v+\Delta v) S_{01}$$
 (9)

and  $S_{01}$  is related to  $S_{10}$  by the detailed balance.

The V-V transition rate coefficients are obtained by using the probability of energy exchange per collision derived by Rapp and Englander-Golden  $^{11}$ . This probability is

$$A_{sm}^{rn} = Sin^{2}(4 \pi \mu LV_{o} U_{rn} U_{sm}/h) Sech^{2}(\frac{2LE_{d}}{V_{o}})$$
 (10)

where  $\mu$  is the reduced mass, L is a characteristic length which enters the exponential of the repulsive potential,  $V_0$  is the velocity of the colliding particle,  $U_{rn}$  is the matrix element for transition between states r and n and  $E_d$  is the energy defect. We shall consider the case of a harmonic oscillator with  $E_d$ =0. The  $Sin^2$  term in Eq. (10) can be approximated by the square of the argument as shown by Fisher and Kummler<sup>2</sup>. With these assumptions, the probability per collison for transitions from v=1 to v=0 can be written as

$$A_{01}^{10} = 16\pi^2 \mu^2 L^2 (U_{01})^4 \frac{V_0^2}{h^2}$$
 (11)

The matrix element for a harmonic oscillator 3 is

$$(U_{01})^2 = (\frac{1}{4L})^2 \frac{h}{\pi M \nu}$$
 (12)

Where M is the mass of an atom and  $\nu$  is the vibrational frequency. Substituting Eq. (12) into (11) and using  $^2$  L = 0.2Å we obtain

$$A_{01}^{10} = 4.0 \times 10^{-2} T_{g}$$
 (13)

Where  $T_g$  is in eV. The rate coefficient for V-V transitions is obtained by multiplying the probability for energy enchange by the collision rate

coefficient i.e.  $\sigma V_0$ . Where  $\sigma$  is the cross section for hard sphere collisions and  $V_0$  is the average velocity. Using a value  $^{12}$  of 3.75% for the diameter of the nitrogen molecule, equation (13), and the average velocity as a function of gas temperature we obtain the necessary rate coefficient.

$$P_{01}^{10} = A_{01}^{10} \sigma V_o = 5.0 \times 10^{-11} (T_q)^{3/2}$$
 (14)

Hence, the V-V transition rates for arbitrary levels, using harmonic oscillator relations<sup>3</sup>, are

$$P_{v+1,v}^{W-1,W} = (v+1)w P_{10}^{01}$$

$$P_{v,v+1}^{W,W-1} = w(v+1) P_{10}^{01}$$
(15)

## 4. RESULTS AND ANALYSIS

and

The master equation discussed in Section II is solved for v=0 to v=32 and as a function of time using a computer. The solutions are carried out for a range of electron densities from  $10^{12} {\rm cm}^{-3}$  to  $10^{15} {\rm cm}^{-3}$  in a 640 Torr of nitrogen. The electron and gas temperatures were different and assumed to have Maxwellian distributions. Three gas temperatures of 0.025eV, 0.25eV and 0.5eV were chosen with electron temperatures of 1.0eV. The results are discussed below.

# 4.1 THE VIBRATIONAL RELAXATION AT $T_q = 0.025 eV$

Figures 2-5 show typical results depicting the population densities of 13 vibrational levels of v = 0 to v = 12 as a function of time for the initial conditions of  $N_2(0) = 2.1 \times 10^{19} \text{cm}^{-3}$ ,  $N_e(10^{12} \text{cm}^{-3} - 10^{15} \text{cm}^{-3})$ ,  $T_e = 1.0 \text{ eV}$  and  $T_g$  = 0.025eV. These figures show that the vibrational levels attain a quasisteady state distribution which signifies the development of a vibrational The establishment of the vibrational distrubution clearly depends on various parameters which determine how fast such a distribution takes place. For example in Figures 2-5 the electron density is varied from  $10^{12} {\rm cm}^{-3}$  to  $10^{15} {\rm cm}^{-3}$ , while the rest of the parameters i.e. the electron and gas temperatures are kept the same. We observe that the vibrational the electron density. This time for  $n_e = 10^{12} \text{cm}^{-3}$ ,  $10^{13} \text{cm}^{-3}$ ,  $10^{14} \text{cm}^{-3}$  and  $10^{15}$  cm<sup>-3</sup> is 2 x  $10^{-4}$  sec, 2 x  $10^{-5}$  sec, 2 x  $10^{-6}$  sec and 2 x  $10^{-7}$  sec, respectively. Under these conditions, the e-V collisions controls the time for the establishment of the vibrational distribution, because at room temperature the V-V transition rates are very small especially for the lower vibrational levels whose population densities are controlled by electron The vibrational distribution time  $\tau_{_{\rm V}}$  reduced approximately an order of magnitude when the electron density is increased by an order of magnitude.

The vibrational distribution as calculated by the master equation can be characterized by a temperature  $\mathcal{F}_{v}$ , where  $\mathcal{F}_{v}$  is deifined by the usual harmonic oscillator relation for a Boltzman distribution i.e.

$$E_{v} = 0.3 \left[ \text{Exp}(\frac{0.3}{T_{v}}) - 1 \right]^{-1}$$
 (16)

Here  $\mathsf{E}_\mathsf{V}$  is the average vibrational energy of the molecule and is obtained by the following relation

$$E_{v} = \frac{\nabla 0.3 \times N_{2}(v)}{\sqrt[3]{v} N_{2}(v)}$$
 (17)

Under the conditions where the T-V and V-V rates are negligible we observe that the vibrational temperature is controlled by electron molecule collisions and that the vibrational temperature, as defined above, approaches the electron temperature as shown in Figure 6. The vibrational temperature becomes closer to the electron temperature for higher electron densities. The calculated densities of the vibrational levels are in Boltzmann equilibrium for the mid vibrational levels, slightly higher than Boltzmann for the lower levels and underpopulated for levels closer to the dissociation limit. This under population is partially due to the neglect of the three-body neutral recombination to different vibrational levels and partially to the ease of dissociation from such high levels.

The population density of level 32, i.e., the number of molecules dissociated, is shown in Figure 7 as a function of time for the same range in the electron density  $(10^{12} {\rm cm}^{-3} - 10^{15} {\rm cm}^{-3})$ . An obvious feature in Figure 7 is that the higher the electron density the faster is the molecular dissociation. This is due to enhanced collision rates with increased electron density.

## 4.2 THE VIBRATIONAL RELAXATION AT ELEVATED GAS TEMPERATURE

In this section we present the relaxation calculations for two nitrogen

gas tempertures of 0.25eV and 0.50eV where the effects of V-T and V-V can be seen more effectively.

Figures 8-11 show the population densities of thirteen vibrational levels v=0 to v=12 for  $T_{\rm g}$  = 0.25eV and electron densities of  $10^{12}{\rm cm}^{-3}$  to  $10^{15}{\rm cm}^{-3}$ . The vibrational distribution is developed in time scales of  $10^{-4}$ sec,  $2x10^{-5}$ sec,  $2x10^{-6}$ sec and  $2x10^{-7}$  for  $N_0 = 10^{12}$ cm<sup>-3</sup>,  $10^{13}$ cm<sup>-3</sup>,  $10^{14}$ cm<sup>-3</sup> and  $10^{15}$ cm<sup>-3</sup>, respectively. These times are not different from those presented in Section 4.1 for  $T_{c} = 0.025 \text{eV}$  indicating that electron-molecule collisions and V-V transitions are still dominant in establishing the vibrational equilibrium. The vibrational temperatures for these distributions are shown in Figure 12. It is interesting to observe that these temperatures are lower for each electron density compared with those shown in Figure 6. Thus the T-V and V-V processes apparently depress the vibrational temperature compared to the temperature obtained from purely e-V processes. This is because the deexcitation rates for T-V and V-V are larger than the corresponding rates at  $T_{\mathbf{q}}$ = 0.025 eV. Furthermore, the vibrational levels are in near Blotzmann distribution for the lower and mid levels while the levels near the dissociation limit are underpopulated compared to Boltzmann relation at the derived temperature.

At a gas temperature of 0.5eV, the results are much different than those at  $T_g = 0.25$  eV. For example, the vibrational distribution is established at times of  $2 \times 10^{-6} {\rm sec}$ ,  $3 \times 10^{-6} {\rm sec}$ ,  $7 \times 10^{-7} {\rm sec}$  and  $2 \times 10^{-7} {\rm sec}$  for  $n_e = 10^{12} {\rm cm}^{-3}$ ,  $10^{13} {\rm cm}^{-3}$ ,  $10^{14} {\rm cm}^{-3}$ , and  $10^{15} {\rm cm}^{-3}$  respectively as shown in Figures 13-16. These times are much shorter compared to those obtained at lower gas temperature, especially for lower electron densities which implies that V-T and V-V are now comparable and even higher than the e-V rates for lower electron densities. The vibrational temperatures, obtained with Eqs. 16 and

17 which characterize the development of the vibrational distributions are shown in Figure 17. Again, the vibrational temperatures are lower compared to those for lower gas temperatures. The level populations near the dissociation limit as before, are underpopulated compared to a Boltzmann distribution at the calculated  $T_{\rm V}$ . The mid level populations are near Blotzmann and the lower levels are slightly overpopulated.

## 4.3 THE T-V AND V-V EFFECTS ON THE VIBRATIONAL DISTRIBUTION FOR A FIXED No.

For an electron density of  $10^{12} \text{cm}^{-3}$ , the case of low electron density, the evolution of the vibrational temperature for three gas temperatures is shown in Figure 18. The following observation can be made; (a) the vibrational distribution is established faster for higher gas temperatures because of the enhanced V-V and T-V rates (b) the vibrational temperature is lower for higher gas temperatures because V-V and T-V processes tend to depress the vibrational level populations (c) the gas temperature effects are different depending on whether  $T_g$  is low or high. For example, at  $T_g$ =0.25eV the vibrational temperature is depressed more compared to that for  $T_g$ =0.5eV. This is because the V-T deexcitation rates are not compensated by the inverse excitation processes.

## 4.4 THE DISSOCIATION RATE

In the computer solution of the master equation, level 32 designated the number of molecules dissociated under the total actions of e-V, V-V and V-T processes. An overall dissociation rate under these conditions can be obtained by defining the dissociation rate,  $K_d$ , in the following manner

$$K_{d} = \frac{dN_{2}(32)/dt}{\xi N_{2}(v)}$$
 (18)

This expression slightly over estimates the dissociation rate since we do not account for the three body atomic recombination into molecules. Figure 19 shows the dissociation rate using Eq. 18 for  $N_{\rm e}$  =  $10^{12}$  and three gas temperatures. The quasi steady state dissociation rates represented by the plateaus in Figure 19 show a very interesting result. The dissociation rate for the gas at the room temperature is higher than the dissociation rate when  $T_q > 0.025$  eV. On the other hand, the dissociation rate when  $T_q = 0.25$ eV is lower than when  $T_{\boldsymbol{q}}$  is 0.5eV. To understand this behaviour one can look at the vibrational temperature under these conditions (see Figure 20) where for higher dissociation rates one also has higher vibrational temperatures. This implies that the higher vibrational states are highly populated which then are To further understand the contributions of various easily dissociated. processes to the overall dissociation rate consider for example Figure 21. In this Figure, we see that for  $T_q = 0.5eV$  the dissociation rate, when all physical processes are included, is given by graph (a) and indicates a value of 40  $\sec^{-1}$ . However, when one turns off the e-V processes, the dissociation rate, given by graph (b), is practically unchanged compared to graph (a). This implies that for low electron density (in this case  $N_e = 10^{12} cm^{-3}$ ), the V-V and T-V processes dominate at  $T_{\alpha}$  = 0.5eV. When we turn off the T-V processes, the dissociation rate is the highest with a value of 400 sec<sup>-1</sup> and is indicated by graph (c) which implies that V-V processes contribute predominately to the dissociation. On the other hand, when we turn off the

V-V processes the dissociation rate given by graph (d) indicates a value of  $2.5 \times 10^{-1} {\rm sec}^{-1}$  which is much smaller than the previous rates discussed above. Finally when we turn off both V-V and T-V processes we obtain a dissociation rate of  $\sim 4.5 \times 10^{-1} {\rm sec}^{-1}$ , indicated by graph (e). This implies that at an electron temperature of 1.0eV and a gas temperature of 0.5eV the dissociation rate due to electron molecule collisions alone is equal to the dissociation rate due to T-V processes with one exception, that is, the establishment of the vibrational distribution and the molecular dissociation occurs much faster with V-T transitions compared to that with only e-V processes (see Figure 22).

However, the dissociation rates for electron densities higher than  $10^{12} {\rm cm}^{-3}$  are shown in Figures 23 and 24. Where for N<sub>e</sub> = $10^{13} {\rm cm}^{-3}$  we observe the rate of dissociation at  $T_q = 0.25$  eV to be below that for  $T_q = 0.025$  but very close to it while for  $N_e = 10^{14} cm^{-3}$  the dissociation rate for  $T_q = 0.25 eV$ exceeds that for  $T_{\alpha} = 0.025 \, \text{eV}$ . In general, the higher the vibrational temperature the higher is the dissociation rate as can be seen in Figures 25 and 26. One exception here is the higher dissociation rate for  $T_g = 0.25$ compared to that for  $T_g$  = 0.025 at an electron density of  $10^{14} cm^{-3}$  where the vibrational temperature is higher for  $T_q$  = 0.025 compared to that for  $T_q$  = 0.25 (see Fig. 26). The physical explanation for this is that the higher vibrational levels near the dissociation limit are affected drastically by T-V and V-V processes which are generally depressing in nature i.e., they tend to relax the levels downwards. This downward trend is more than offset by the large rate of electron molecule collisions for  $N_{\rm e}$  =  $10^{14} {\rm cm}^{-3}$  while at  $T_{\rm g}$  = 0.25 these two processes barely compensate each other because of increased VT rates.

Finally, it is of interest to show that the vibrational levels will start

to decay with increased dissociation beyond the steady state. This situation is demonstrated in a typical example in Figure 27.

## 5. ELECTRON IMPACT DISSOCIATION OF N2

The electron impact dissociation of nitrogen has been measured by Winters  $^{13}$ . More recently however, Zipf and McLaughlin  $^{14}$  have performed a more comprehensive study of the electron impact dissociation. This study has delineated the basic processes and the states that contribute to the dissociation. It is concluded that all singlet states (~54 states) of the  $^1\pi$  and  $^1\Sigma$  manifolds and in the energy range of 12.5 - 14.8 eV predissociate completely. Furthermore, the sum of the excitation cross sections for these states comprises 60% of the total dissociation cross section measured by Winters  $^{13}$ . The rest of the dissociation arises as a result of excitation to levels higher than 14.8 eV.

The various inelastic electron impact scattering studies  $^1$  on  $N_2$  and the extreme ultraviolet absorption measurements  $^2$  have indicated that nitrogen possesses a large number of singlet states in the range of  $11.5-40\,\mathrm{eV}$ . These states are generally characterized as Valence and Rydberg like with life times in the range of  $1-100\,\mathrm{nsec}$ . Hence it is expected that these states emit considerable amount of radiation in the extreme ultraviolet. However, because of the predissociation of these states the euv emission will be minimal. The reabsorption of these radiations also contributes to the dissociation of the molecule  $^{14}$ ,  $^{17}$ .

Thus the total dissociation cross section for  $N_2$  as illustrated by Zipf and McLaughlin includes the contribution from states above 14.8 eV which includes dissociation leading to excited nitrogen atoms, states with 17.3 eV peak from Lassettre's data  $^{15}$ , Rydberg states, triplet states above 11 eV, and

part of the  $a^1\pi_g$  state. The dissociation cross section for the optically thin and thick cases are obtained and are in good agreement with Winters' measurement<sup>13</sup>. These cross sections are averaged over a Maxwellian electron velocity distribution and the dissociation rates have been obtained<sup>9,14</sup>. From these one observes that the dissociation rate coefficient for electrons with  $T_e = 1.0 \text{ eV}$  is  $1.4 \times 10^{-13} \text{ cm}^3/\text{sec}$ . Accordingly, the dissociation rate due to this process alone is  $1.4 \times 10^{-1} \text{sec}^{-1}$  for  $N_e = 10^{12} \text{ cm}^{-3}$  at room temperature compared to a rate of dissociation of 240  $\text{sec}^{-1}(\text{see Fig. 19})$  due to the vibrational ladder route as in the model discussed in the paper. For  $N_e = 10^{14}$  and  $T_g = 0.025$  the corresponding rates are 14  $\text{sec}^{-1}$  and 1500  $\text{sec}^{-1}$ , respectively, indicating that the ladder climbing enhances the moleuclar dissociation.

In conclusion, we have provided a model for the molecular dissociation in a nitrogen discharge with a low degree of ionization where basic processes resulting in the dissociation are delineated. We plan to include the effect of an harmonicity to this model in the future. However, we are currently in the process of completing a new vibrational dissociation model due to the interaction of high energy electron beam with  $N_2$  where the relevant temperatures are calculated from the first principles and are not held fixed as the model in this paper.

# VIBRATIONAL EXCITATION RATE COEFF.

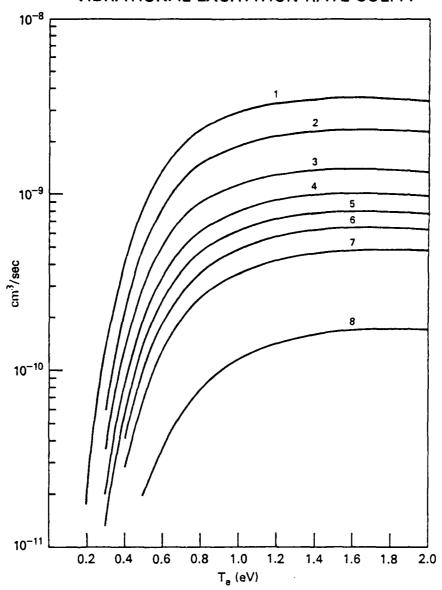


Fig. 1 Electron Impact Excitation Rate Coefficents for eight Nitrogen ground state vibrational levels

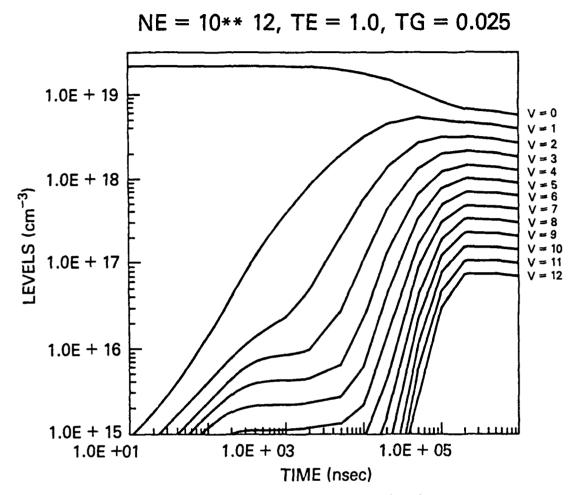


Fig. 2 Vibrational State Densities for N<sub>e</sub> =  $10^{12}$ cm<sup>-3</sup>, T<sub>e</sub> = 1.0 eV, and T<sub>g</sub> = 0.025 eV

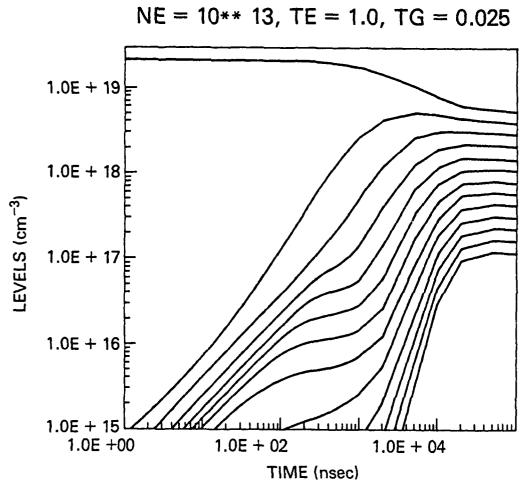


Fig. 3 Vibrational State Densities for  $N_e = 10^{13} cm^{-3}$ ,  $T_e = 1.0 eV$  and  $T_g = 0.025 eV$ 

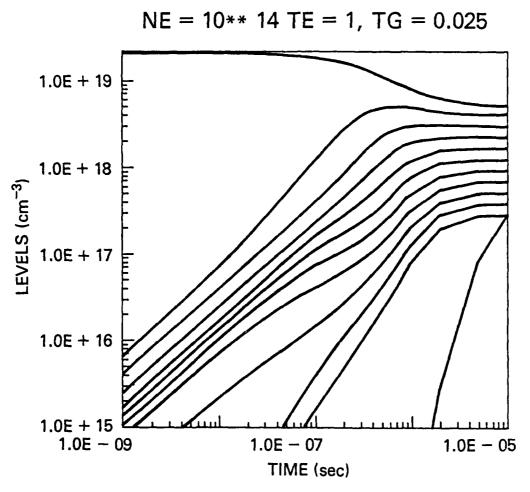


Fig. 4 Vibrational State Densities for  $N_e = 10^{14} cm^{-3}$ ,  $T_e = 1.0 eV$  and  $T_g = 0.025 eV$ 

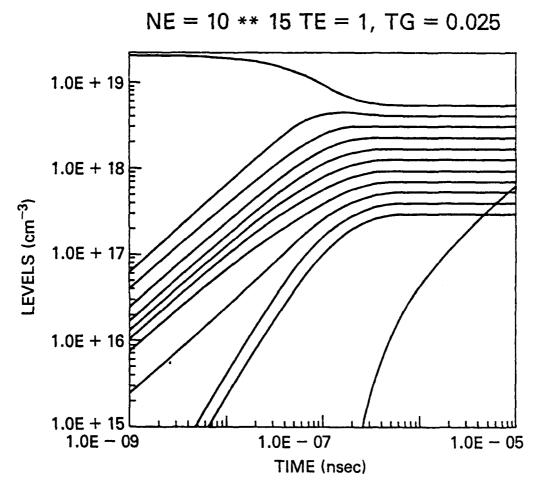


Fig. 5 Vibrational State Densities for  $N_e = 10^{15} \text{cm}^{-3}$ ,  $T_e = 1.0 \text{ eV}$  and  $T_g = 0.025 \text{ eV}$ 

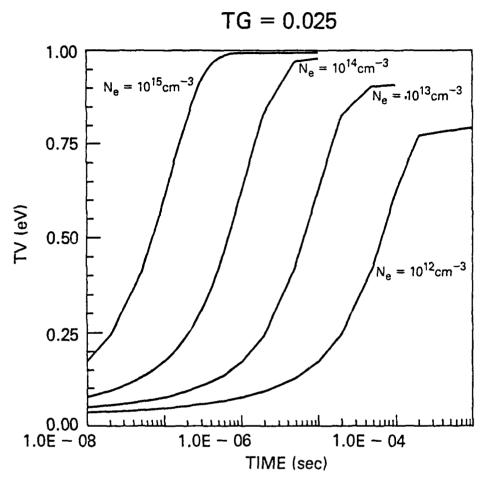


Fig. 6 The Vibrational Temperature for Te = 1.0 eV, Tg = 0.025 eV and Ne =  $10^{12} {\rm cm}^{-3}$  -  $10^{15} {\rm cm}^{-3}$ 

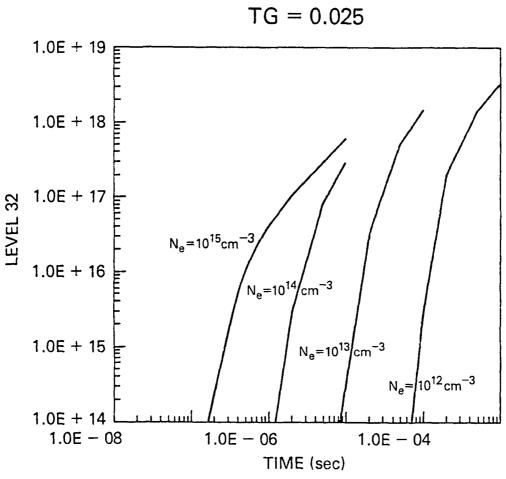
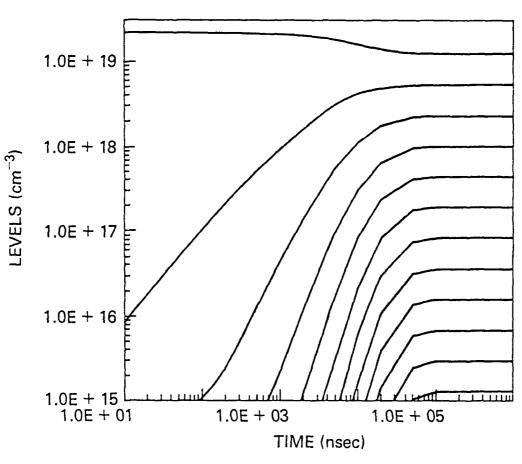


Fig. 7 Population Density of the Dissociated Molecules for  $T_e$  = 1.0 eV,  $T_g$  = 0.025 eV and  $N_e$  =  $10^{12} cm^{-3}$  -  $10^{15} cm^{-3}$ 

NE = 10 \*\* 12, TE = 1.0, TG = 0.25



ľ.

Fig. 8 Vibrational State Densities for  $N_e = 10^{12} cm^{-3}$ ,  $T_e \approx 1.0$  eV and  $T_g \approx 0.25$  eV

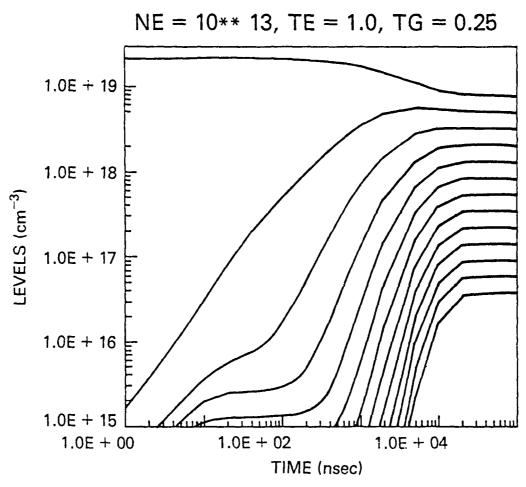


Fig. 9 Vibrational State densities for  $N_e = 10^{13} cn^{-3} m T_e = 1.0$  eV and  $T_g = 0.25$  eV



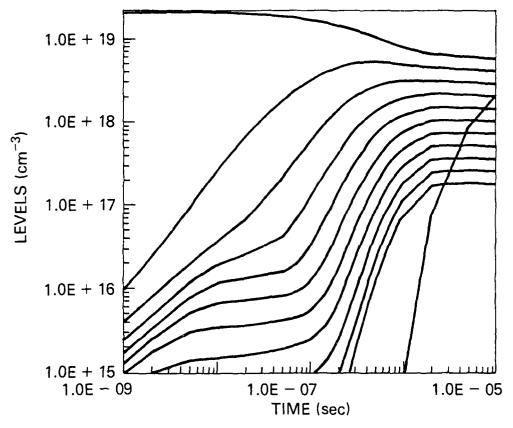


Fig. 10 Vibrational State Densities for  $N_e = 10^{14} cm^{-3}$ ,  $T_e = 1.0$  eV and  $T_g = 0.25$  eV

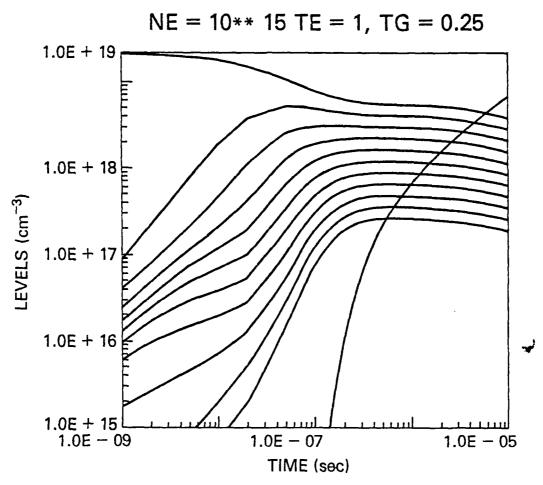


Fig. 11 Vibrational State Densities for  $N_e = 10^{15} cm^{-3}$ ,  $T_e = 1.0$  eV and  $T_g = 0.25$  eV

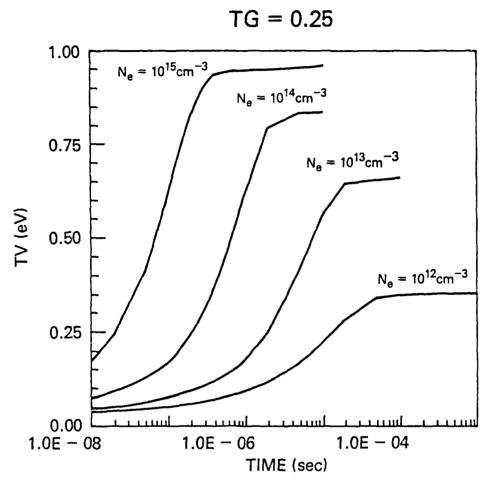


Fig. 12 The Vibrational Temperature for T  $_{e}$  = 1.0 eV, T  $_{g}$  = 0.25 eV and N  $_{e}$  =  $10^{12} \rm cm^{-3}$  -  $10^{15} \rm cm^{-3}$ 



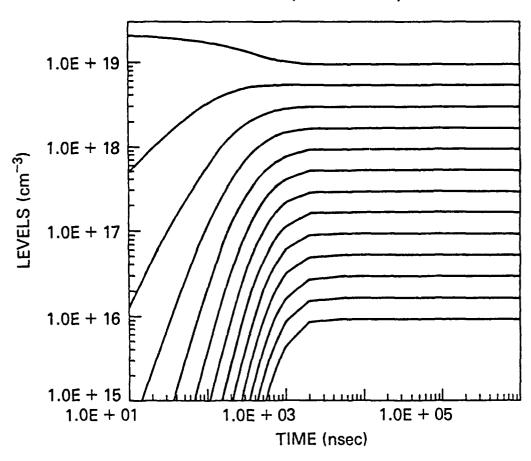


Fig. 13 Vibrational State Densities for  $N_e = 10^{12} cm^{-3}$ ,  $T_e = 1.0 eV$  and  $T_g = 0.5 eV$ 

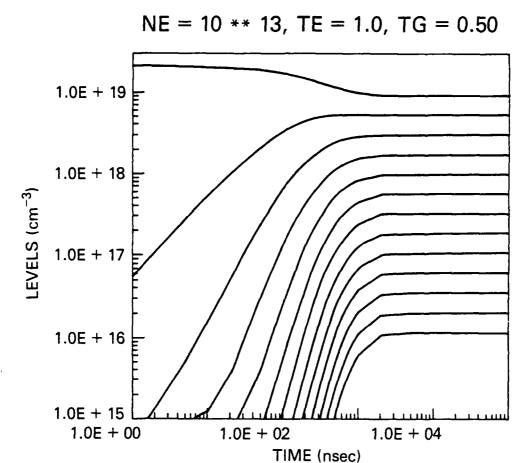


Fig. 14 Vibrational State Densities for N<sub>e</sub> =  $10^{13}$ cm<sup>-3</sup>, T<sub>e</sub> = 1.0 eV and T<sub>g</sub> = 0.5 eV

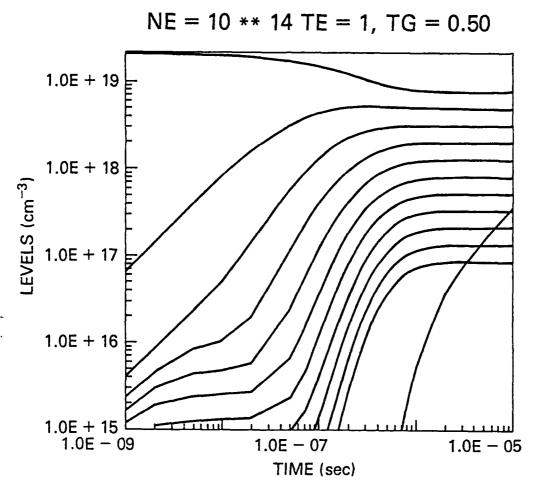


Fig. 15 Vibrational State Densities for  $N_e = 10^{14} cm^{-3}$ ,  $T_e = 1.0 eV$  and  $T_g = 0.5 eV$ 

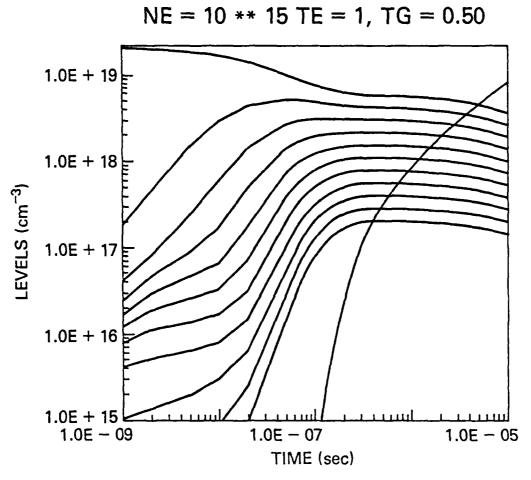


Fig. 16 Vibrational State Densities for  $N_e = 10^{15} cm^{-3}$ ,  $T_e = 1.0 eV$  and  $T_g = 0.5 eV$ 

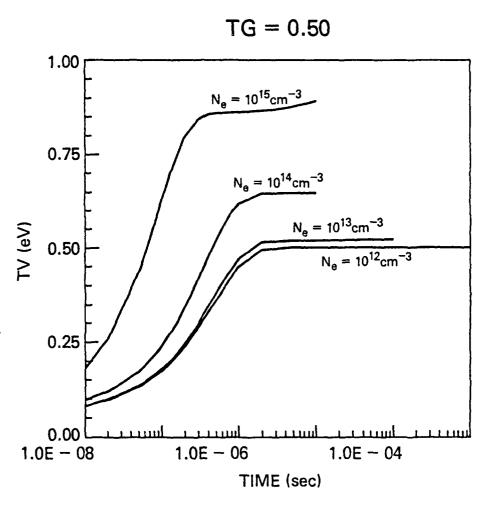


Fig. 17 The Vibrational Temperature for  $T_e$  = 1.0 eV,  $T_g$  = 0.5 eV and  $N_e$  =  $10^{12} cm^{-3}$  =  $10^{15} cm^{-3}$ 

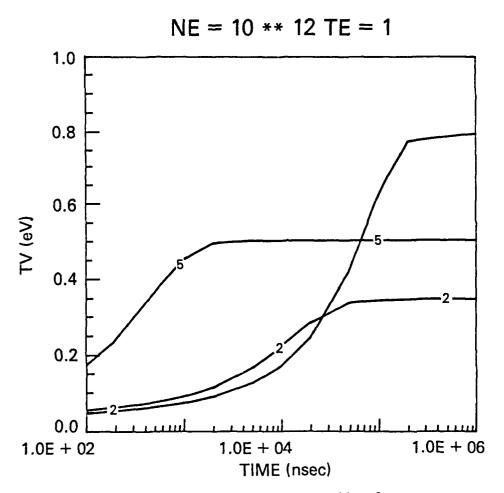


Fig. 18 The Vibrational Temperature for N<sub>e</sub> =  $10^{12}$ cm<sup>-3</sup>, T<sub>e</sub> = 1.0 eV and T<sub>g</sub> = 0.025 eV, 0.25 eV and 0.5 eV

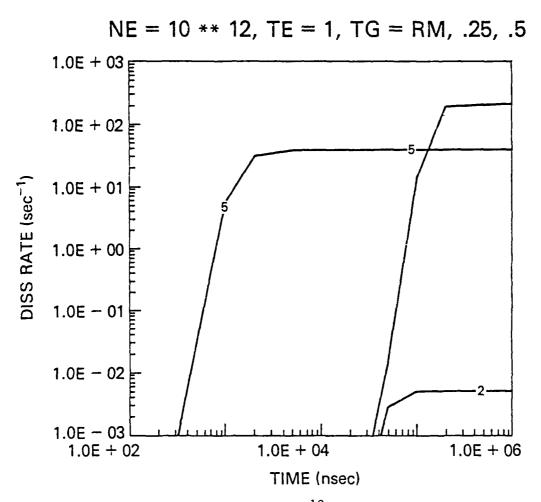


Fig. 19 The Dissociation Rate for  $N_e = 10^{12}$ ,  $T_e = 1.0$  eV and  $T_g = 0.025$  eV, 0.25 eV and 0.5 eV

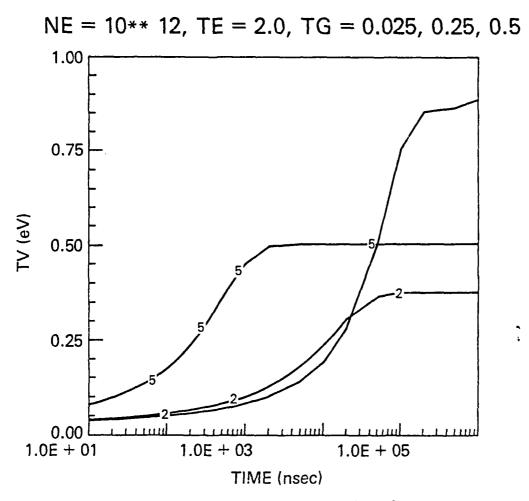


Fig. 20 The Vibrational Temperature for N<sub>e</sub> =  $10^{12}$ cm<sup>-3</sup>, T<sub>e</sub> = 1.0 eV and T<sub>g</sub> = 0.025 eV, 0.25 eV and 0.5 eV

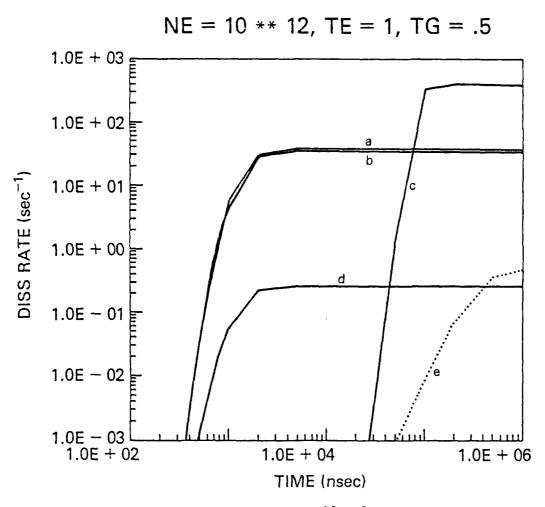


Fig. 21 The Dissociation Rate for  $N_e = 10^{12} cm^{-3}$ ,  $T_e = 1.0$  eV and  $T_g = 0.5$  eV (a) all processes, (b) V-V and V-T only (c) e-V and V-V only (d) e-V and T-V only (e) e-V only

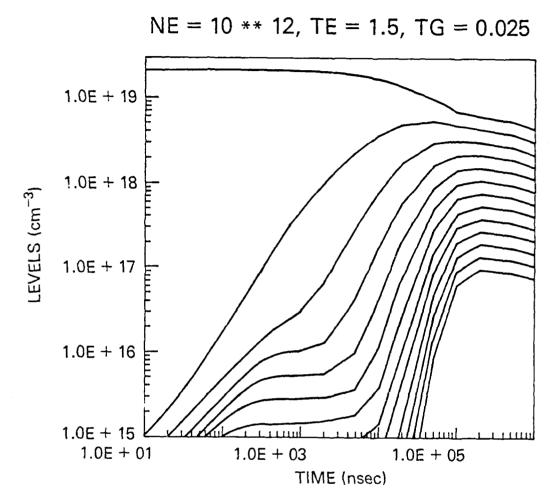


Fig. 22 Vibrational State Densities for  $N_e = 10^{12} cm^{-3}$ ,  $T_e = 1.0$  eV and  $T_g = 0.025$  where only e-V processes are considered

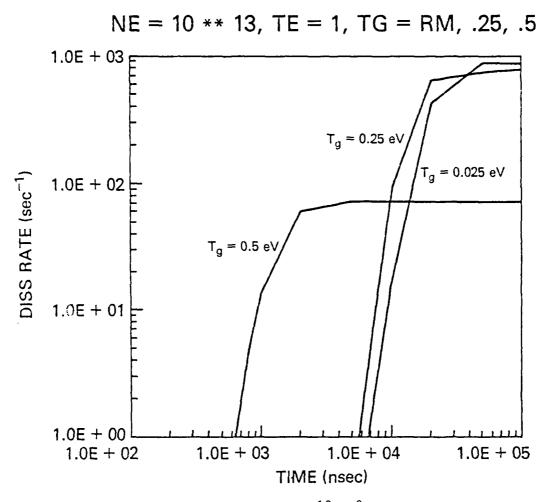


Fig. 23 The Dissociation Rate for N<sub>e</sub> =  $10^{13}$ cm<sup>-3</sup>, T<sub>e</sub> = 1.0 eV and T<sub>g</sub> = 0.025 eV, 0.25 eV and 0.5 eV

NE = 10 \*\* 14, TE = 1.0, TG = RM, .25, .5

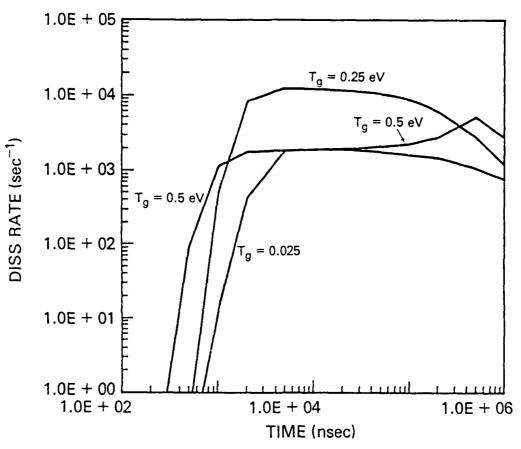


Fig. 24 The Dissociation Rate for N<sub>e</sub> =  $10^{14}$ cm<sup>-3</sup>, T<sub>e</sub> = 1.0 eV and T<sub>g</sub> = 0.025 eV, 0.25 eV and 0.5 eV

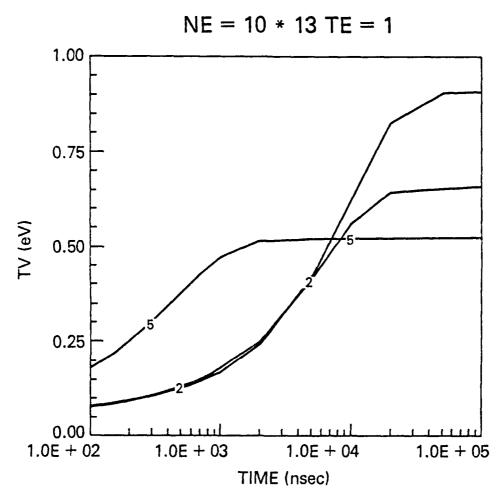


Fig. 25 The Vibrational Temperature for N $_{\rm e}$  =10 $^{13}$ cm $^{-3}$ , T $_{\rm e}$  = 1.0 eV and T $_{\rm g}$  = 0.025 eV, 0.25 eV and 0.5 eV

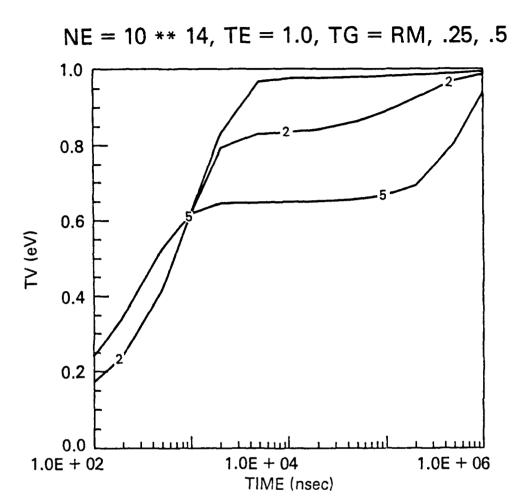
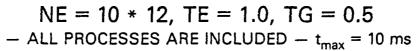


Fig. 26 The Vibrational Temperature for N<sub>e</sub> =  $10^{14}$ cm<sup>-3</sup>, T<sub>e</sub> = 1.0 eV and T<sub>g</sub> = 0.025 eV, 0.25 eV and 0.5 eV



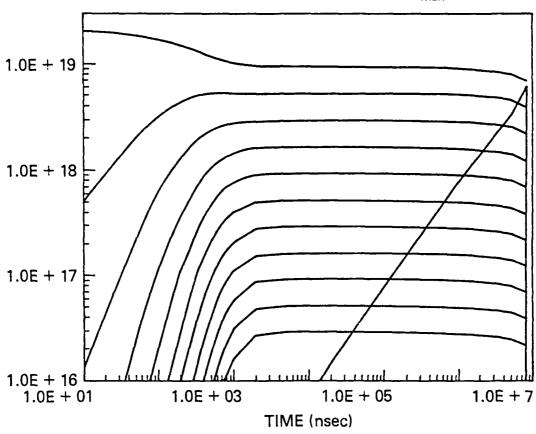


Fig. 27 Vibrational State Density for  $N_e=10^{12} {\rm cm}^{-3}$ ,  $T_e=1.0~{\rm eV}$  and  $T_g=0.5~{\rm eV}$ . The steady state and the decay are indicated.

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